# Assessing Combinational Generalization of Language Models in Biased Scenarios

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## Abstract

In light of the prominence of Pre-trained Language Models (PLMs) across numerous downstream tasks, shedding light on what they learn is an important endeavor. Whereas previous work focuses on assessing in-domain knowledge, we evaluate the generalization ability in biased scenarios through component combinations where it could be easy for the PLMs to learn shortcuts from the training corpus. This would lead to poor performance on the testing corpus, which is combinationally reconstructed from the training components. The results show that PLMs are able to overcome such distribution shifts for specific tasks and with sufficient data. We further find that overfitting can lead the models to depend more on biases for prediction, thus hurting the combinational generalization ability of PLMs.

# 1 Introduction

Transformer-based (Vaswani et al., 2017) pretrained Language Models (PLMs) have enabled substantial performance gains across numerous downstream tasks (Devlin et al., 2019; Brown et al., 2020). To evaluate PLMs, existing work largely follows the scheme of sampling training and test data from the same distribution. In reality, given the productivity of human language, humans are widely assumed to interpret new linguistic utterances based on some notion of compositionality (Chomsky, 2006; Baroni, 2020).

In this paper, we want to investigate to what extent models are prone to using biases for prediction and how this may affect their performance on unseen instances requiring combinational inference. This relates to their generalization ability, which is regarded as a key challenge in building human-like models (Bommasani et al., 2021). We propose a

Training data: You should watch it. It is great This movie is bad. It is terrible							
ID: It is worthwhile to watch this movie. It is							
COOD:	OOD: It is worthwhile to watch this movie. It is terri						
OOD:	DOD: It is worthwhile to watch this movie. It is oka						
	Label 1	Label 2	Label 3				
Label 1	0	1	1	Column: Label in Template			
Label 2	1	0	1	Row: Original Label			
Label 3	1	1	0				

Figure 1: Example of data induction for 3-way sentiment classification. The top shows two training instances. The below part shows three generated instances (**ID**: In-Distribution, **COOD**: combinational Out-Of-Distribution, **OOD**: Out-Of-Distribution). In the table, labels in red are the combinations used for training and ID, whereas black and blue labels are used in the test set. *Blue* ones (COOD) can be inferred from the training data, while *black* ones (OOD with Label 3 in Template) cannot be combinationally inferred because the training set does not include such template.

method to assess a PLM's generalization capacity in classification tasks that require combinational generalization to overcome biases in the training data. Specifically, we modify an original dataset by recombining components of training data points to form unseen test data. Figure 1 provides a brief illustration of the principle. Based on the training data, the model can easily classify the ID instances. However, since we introduce a scenario with special hidden biases, a PLM that only picks up such training data biases would fail on the COOD instances in the test set. To handle those correctly, the combinational inference is required, i.e., drawing conclusions based on smaller fragments of text observed during training. Finally, there are also truly challenging genuine OOD instances that are not easily combinationally inferrable. Details of the hidden bias scenario are given in the bottom part

of Figure 1 as well as later on in Section 3. Overall, our results suggest that PLMs possess excellent generalization abilities and avoid succumbing to the risky form of bias introduced in the training data. However, the performance depends on the task and data size.

## 2 Related Work

**Probing Pre-trained Models.** Numerous studies attempt to shed light on how PLMs learn (Rogers et al., 2020). Beyond understanding linguistic structures and semantics (Hewitt and Manning, 2019; Tenney et al., 2019) as well as world knowledge (Li et al., 2021), some studies show that PLMs possess a strong generalization ability across similar tasks and in out-of-distribution detection (Hendrycks et al., 2020; Utama et al., 2020; Chen et al., 2021; Geng et al., 2022).

Most prior work assesses PLMs based on the setting of test and training data stemming from the same distribution. This yields insights on standard in-task or in-domain learning, while in our work we are interested in the type of more generalizable knowledge acquired from the in-task training data. This relates to the robustness of PLMs, as the model can only do well on our test data if it pays attention to all components of the data rather than falling prey to biases in the training data.

**Combinational Generalization.** The combinational generalization here refers to the model's ability to properly handle unseen data samples consisting of fragments observed during training, and regard combinational generalization as a part of compositional generalization. Some studies investigate the compositional features and inductive biases of neural net models for sequence-to-sequence and generation tasks (Liska et al., 2018; Lake and Baroni, 2018), mostly at the phrase level, while we consider encoder models for classification tasks and focus on compositional inference connecting entire sentences.

One similar work is R&R (Akyürek et al., 2021), which also constructs data from fragments of training data. The major difference is that they incorporate the constructed data into training, while we use it for COOD evaluation.

**Prompt-based Tuning.** Prompt tuning has been proposed to reduce the gap between pre-training and fine-tuning on downstream tasks (Brown et al., 2020; Scao and Rush, 2021). It often involves

adding templates to the data and predicting label names at the position of the [MASK] token (Schick and Schütze, 2021b,a). Inspired by prompt engineering, our work also involves the use of template engineering. However, we do not invoke them to elicit a PLM's prior knowledge, but as a core part of the input semantics. Additionally, finding the best templates and label names is not our focus, so we have not investigated automated prompt identification techniques (Shin et al., 2020; Gao et al., 2021), but we demonstrate that our results are coherent across different templates and label names.

## **3** Approach

#### 3.1 Data Induction

Given an original training dataset  $\mathcal{D}$  consisting of (x, y) pairs, where x is a training instance and y is its corresponding label, we induce a new dataset  $\hat{\mathcal{D}}$ . The latter consists of  $(\hat{x}, \hat{y})$  pairs, created by adding templates and generating new labels based on  $\mathcal{D}$ . Each  $\hat{x} = x \oplus t$  is a combination of an x and a template t appended at the end of x. For a general template "It is <label>", the <label> is replaced by the task-specific label names, so there are |Y| unique templates for each unique label  $y_t$ . For example, if the task is sentiment classification, there could be templates "It is positive", "It is negative", and possibly "It is neutral". If  $y_t$  in the template t is consistent with the original label y, the new label  $\hat{y}$  is 0, otherwise, it is 1.

To evaluate a PLM's generalization ability for combinational generalization, a biased scenario is constructed based on  $\hat{D}$ . The model could easily just learn shortcuts from the training data, without accounting for generalization. The training data excludes certain kinds of combinations of inputs and templates as shown in Fig. 1, so these combinations are unseen when fine-tuning the PLM, but it may still be possible for the model to infer them compositionally from parts of the training data. This is what we assess in this paper.

**Example.** To help illustrate how to construct the biased data, we take the task of Natural Language Inference (Williams et al., 2018) as an example. We select K data points x for each label as training data. For data x with label y = ENTAILMENT or CONTRADICTION, we concatenate x with corresponding consistent templates and add label  $\hat{y} = 0$  (2K instances). If a model only observed these specific combinations, it would be prone to picking

up the bias and misunderstanding combinations of the same x with another t. For further K instances of x with y = NEUTRAL, we append two inconsistent templates to construct the  $\hat{x}$ . This yields another 2K data points with  $\hat{y} = 1$  and leads to a balance between instances with labels 0 and 1 (2K instances each) in the training dataset. The test set will then also ask for new combinations.

## 3.2 Main Results

## 3.3 Fine-tuning

Given a data instance  $(\hat{x}, \hat{y})$  from  $\hat{D}$  such that  $\hat{x} = x_i \oplus t_i$ , we invoke the PLM to obtain a representation  $\operatorname{enc}_{\theta} = \operatorname{Encoder}_{\theta}(x_i \oplus t_i)$ , where  $\theta$  are the model parameters. Next, a linear classifier  $w \in \mathbb{R}^{d \times 2}$  where d is the representation size for [CLS] is trained by optimizing the objective:

$$\operatorname{argmax}_{\theta} P(\hat{y}_i \mid w \cdot \operatorname{enc}_{\theta}([\mathsf{CLS}])) \\ = \operatorname{argmax}_{\theta} \frac{\exp(w_{\hat{y}_i} \operatorname{enc}_{\theta}([\mathsf{CLS}]))}{\sum_{\hat{y}' \in \{0,1\}} \exp(w_{\hat{y}'} \operatorname{enc}_{\theta}([\mathsf{CLS}]))},$$

where  $\operatorname{enc}_{\theta}([\operatorname{CLS}])$  is the vector for [CLS],  $w_{\hat{y}}$  denotes the softmax scores for  $\hat{y} \in \{0, 1\}$ .

## 4 **Experiments**

#### 4.1 Experimental Setup

**Training details.** We consider the pre-trained versions of BERT (Devlin et al., 2019) and RoBERTa (Liu et al., 2019). For efficiency, we disregard sentences of over 100 tokens<sup>1</sup>. The batch size is 32 for base models and 8 for large models. The learning rate is  $1 \times 10^{-5}$  for all models. The evaluation metric we use is accuracy.

**Datasets.** For our assessment, we rely on Yelp reviews (Zhang et al., 2015) and MNLI (Williams et al., 2018), which each have 3 labels.<sup>2</sup> The label inventories are listed in Table 1.

The main results are reported in Table 2 for K = 2,000. The notation A/B refers to the original dataset A adapted with template B. If A and B are consistent, the label is 0. If not, the label is 1.

The primary observation is that COOD generalization succeeds on Yelp-reviews but does not work as well for MNLI. MNLI is intrinsically harder than Yelp sentiment classification, yet the ID accuracy is high for both MNLI and Yelp. We conjecture that COOD generalization can succeed when the model can straightforwardly infer the label from the semantics of fragments of the input. In addition, we determine that the size of training data may be a factor affecting results in the following analysis (details in Section 5.1).

Second, all PLMs achieve low scores for OOD prediction. This suggests that, as expected, PLMs can, in this case, only use their learned bias to make predictions on such OOD instances. But larger models, such as RoBERTa<sub>Large</sub>, can achieve better COOD and OOD scores than smaller models over all tasks. This may indicate that larger models may have better generalization capacity.

## 5 Discussion

# 5.1 How Do Training Data and Parameter Count Affect the Model?

There is a consensus that more training data coupled with a larger parameter count tends to benefit models for ID tests. So it is worth investigating whether these factors can also contribute to combinational generalization.

Regarding the number of parameters, as Table 2 shows, bigger models obtain better results on COOD and ID data. This finding illustrates that powerful models fit the source domain better and may exhibit stronger combinational generalization.

As for data quantities, we evaluated RoBERTa<sub>Base</sub> and RoBERTa<sub>Large</sub> with different K and plotted the results in Figure 3. Our observation is that both the ID and COOD accuracy are proportional to K. Yet, compared with ID, the performance of COOD is more vulnerable to the data size, while the OOD results remain low. This demonstrates that the training size can influence a model's generalization, but we can also observe the performance gap between ID and COOD closes as K increases. Compared with Yelp, MNLI appears to be more challenging in terms of generalization.



Figure 2: Results of BERT<sub>Base</sub> (left) and RoBERTa<sub>Base</sub> (right) on Yelp for K = 3,000.

<sup>&</sup>lt;sup>1</sup>This applies to the sum of the length of premise and hypothesis for MNLI.

 $<sup>^{2}</sup>$ To achieve our combinational probing, note that the number of unique labels should be greater than 2.

Task name	Template	Label names
MNLI	$\langle S \rangle$ It is $\langle LABEL \rangle$	entailment: entailment, neutral: neutral, contradiction: contradiction
Yelp	$\langle \mathrm{S}  angle$ It is $\langle  ext{label}  angle$	positive: great, neutral: okay, negative: terrible

Dataset	Models	ID			COOD		OOD			
		fst/fst	sec/sec	neu/fst	neu/sec	fst/sec	sec/fst	fst/neu	sec/neu	neu/neu
Yelp	1. BERT <sub>Base</sub>	0.904	0.911	0.782	0.822	0.816	0.705	0.204	0.238	0.125
	2. BERT <sub>Large</sub>	0.892	0.885	0.873	0.869	0.812	0.836	0.254	0.297	0.074
	3. RoBERTa <sub>Base</sub>	0.913	0.871	0.838	0.784	0.773	0.754	0.247	0.244	0.054
	4. RoBERTa <sub>Large</sub>	0.939	0.891	0.856	0.872	0.829	0.838	0.332	0.304	0.123
MNLI	5. BERT <sub>Base</sub>	0.865	0.778	0.652	0.654	0.153	0.269	0.112	0.188	0.277
	6. BERT <sub>Large</sub>	0.929	0.855	0.665	0.691	0.129	0.169	0.081	0.140	0.321
	7. RoBERTa <sub>Base</sub>	0.921	0.857	0.756	0.786	0.356	0.239	0.145	0.133	0.314
	8. RoBERTa <sub>Large</sub>	0.922	0.883	0.820	0.885	0.460	0.382	0.263	0.285	0.378

Table 1: The default templates and label names in our experiments.  $\langle S \rangle$  refers to original data.

Table 2: Rows 1–4 report the main results on Yelp, while rows 5–8 provide results on MNLI. fst: positive/entailment, neu: neutral, sec: negative/contradiction.

Template	Label names	ID	COOD	OOD			
Yelp (positive/neutral/negative)							
$\langle S \rangle$ It is $\langle LABEL \rangle$	great/okay/terrible	0.855	0.761	0.173			
(S) It is (LABEL)         (S) It is (LABEL)         (S) It is (LABEL)	cat/bird/dog train/flight/car terrible/great/okay	0.877 0.881 0.866	0.781 0.763 0.755	0.194 0.182 0.170			
$\begin{array}{l} \langle S \rangle \text{ The sentence is } \langle \text{LABEL} \rangle \\ \langle S \rangle \text{ This sound like } \langle \text{LABEL} \rangle \end{array}$	great/okay/terrible great/okay/terrible	0.863 0.850	0.758 0.764	0.187 0.185			

Table 3: RoBERTa<sub>Base</sub> Performance over Yelp dataset with different templates and label names. K = 2000. The order of label names denotes first and second known class and unknown class

#### 5.2 Analysis of the Effect of Overfitting

Figure 2 depicts how the models perform on Yelp as the number of epochs increases and models increasingly overfit the data. As in Section 3.2, PLMs exhibit excellent performance on ID and COOD tasks and perform poorly on OOD tasks. ID and COOD accuracy both top out in nearly the same epoch, but as the number of epochs continues to increase, the results on COOD decrease more drastically than on ID. This suggests that when PLMs are overfitting, they tend to draw on biases and shortcuts for prediction. Another observation is that OOD accuracy may drop as well as ID and COOD as the number of epochs increase. We hypothesize that at early stages, the knowledge from pre-training still aids in prediction.

## 5.3 Effect of Label Names and Templates

We also compared the impact of different label names and templates. Based on the results shown in Table 3, the selection of label names and templates can affect the results. Even if the label names may not be intuitive, e.g., using label names DOG/CAT/BIRD or switching the order, models may obtain similar ID and COOD accuracy than in the original setting. This result can indicate that the prompt design may have a small impact on performance, as models can adjust to these differences.



Figure 3: Results for different training sizes K. The top two figures show results on MNLI, the bottom two show results on Yelp.

## 6 Conclusion

In this paper, we present a new method to probe the robustness of PLMs when subjected to biased data. Our findings include that (1) PLMs exhibit combinational generalization; (2) the combinational generalization is affected by the training data and parameter count; (3) overfitting is more harmful to a model's generalization ability than in-task ability.

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